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Comparison of Control Performance of Active Mass Damper and Gyroscope System in Active Vibration Control

문영종*	조상원**	윤우현***	이인원****
Moon, Yeong-Jong	*Cho, Sang-Won*	*Yoon, Woo-Hyun*	*Lee, In-Won*

1. Introduction

In recent years, many advanced techniques have been made in modern control theory, and they have been successfully applied to the study of control of a wide variety of engineering systems. Passive and active control schemes are becoming an integral part of the structural systems over the last two decades. A passive control system does not require an external power source. Passive devices, such as base isolation system, viscoelastic dampers and tuned mass damper, are widely accepted by the engineering community as a means for mitigating the effect of dynamic loading on structures. However, these passive device methods are unable to adapt to structural changes and to varying usage patterns and loading conditions.

An active control system is one in which an external source powers control actuators that apply forces to the structures in a manner calculated by control algorithms. In the last two decades, many other active control devices have been developed and conducted by many researchers for civil engineering applications. But most of these devices are based on the active mass damper, applied shear forces to the structure. With distinctive properties, the popular one of active control devices used in navigational, aeronautical and space engineering is gyroscope system.

The gyroscope system is commonly used for the attitude control of an unstructured object. The gyroscope system also can be used for vibration control of structured objects like buildings, towers and bridges. The system is effective for bending modes rather than shear modes, because the system utilizes the gyroscopic moment. High-rise buildings and tall towers are generally flexible and therefore vibrations can be easily induced by external forces. The predominant dynamic deformation mode of tower-like structures is the bending mode rather than the shear mode. For this reason, the gyroscopic moment is effective in controlling vibrations in such structures. Furthermore, this system is more compact and has smaller mass than other control devices with the same ability to control.

2. Gyroscope system

A gyroscope system consists of a rotor which can spin freely about its geometric axis. When mounted in a Cardan's suspension (Fig. 1), a gyroscope can assume any orientation, but its mass center must remain fixed in space. The position of the gyroscope at any given instant can be characterized by following angles.

* 한국과학기술원 건설환경공학과, 박사과정
** University of Western Ontario, 박사후 연수과정
*** 경원대학교 산업환경대학원, 교수
**** 한국과학기술원 건설환경공학과, 교수

1) a rotation of the outer gimbal through an angle ϕ about the axis AA', 2) a rotation of the inner gimbal through θ about BB', and 3) a rotation of the rotor through ψ about CC'.

The anlges ϕ, θ and ψ are called the Eulerian angles. Their derivatives $\dot{\phi}$, $\dot{\theta}$ and $\dot{\psi}$ define, respectively, the rate of precession, the rate of nutation and the rate of spin of the gyroscope at the instant considered.

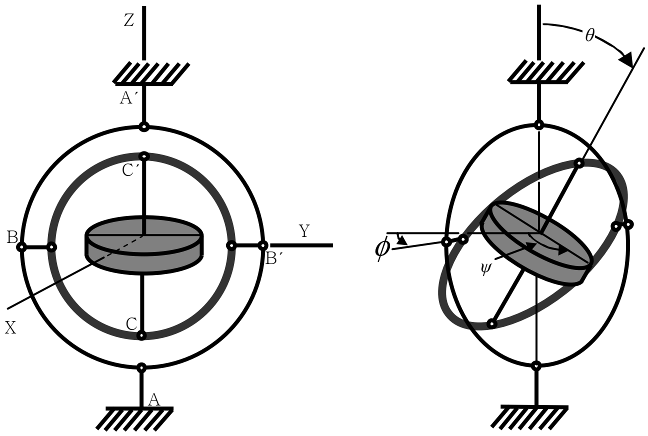


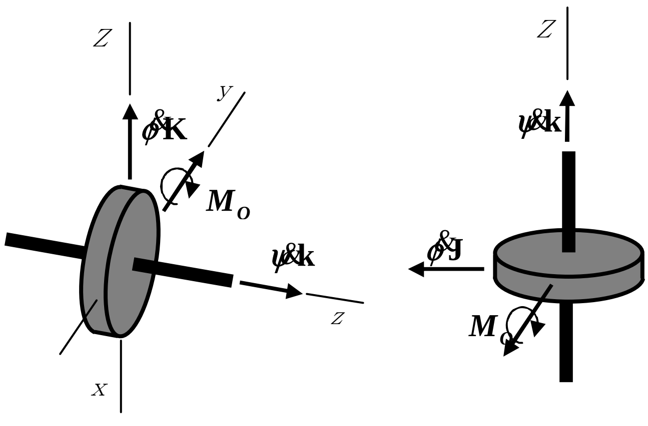
Fig. 1 Gyroscope system

Since θ, $\dot{\phi}$ and $\dot{\psi}$ are constant, the sum of the moments of the required forces reduce to

$$\sum M_O = \left(I\left(\dot{\psi} + \dot{\phi}\cos\theta\right) - I'\dot{\phi}\cos\theta\right)\dot{\phi}\sin\theta\ \mathrm{j} \tag{1}$$

In the particular case when the precession axis and the spin axis are at a right angle to each other, we have $\theta = 90^\circ$ and equation (1) reduces to

$$\sum M_O = I\dot{\psi}\dot{\phi}\ \mathrm{j} \tag{2}$$



(a) (b)

Fig. 2 Particular case of gyroscope system

In actual implementation of gyroscope to the structure, the axis of precession of gyroscope is changed as shown in Fig. 2 (b). Then, equation (2) should be changed to

$$M_Y = I\dot{\psi}\dot{\phi}\cos\phi \quad (3)$$

$$M_Z = I\dot{\psi}\dot{\phi}\sin\phi \quad (4)$$

The moment M_Y is able to control the bending response of the structure of which this actuator is placed, while M_Z acts as a torsional moment on the structure. It is to be noted, however, that it is also possible to eliminate the effect of this torsional moment by using a pair of gyroscope system. The equation of motion can be expressed as

$$M\ddot{x}(t) + C\dot{x}(t) + Kx(t) = \Gamma u(t) + \Lambda f(t) \quad (5)$$

$$u(t) = GM_Y(t) \quad (6)$$

where G is the transformation matrix from the control moment to the equivalent shear force.

3. Numerical Simulation Results

To evaluate the control performance of gyroscope system, numerical examples are considered in which a model of 2.5m cantilever beam is controlled with AMD or gyroscope system.

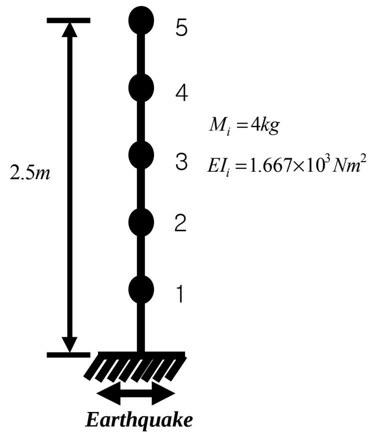


Fig. 3 Numerical Model for Cantilever Beam

In simulation, the model of the structure is subjected to the four earthquakes, El Centro, Hachinohe, Gebze and Mexico earthquake. Because the model considered is a scaled model, the amplitude of the earthquakes was scaled to ten percent of the full scale earthquakes.

To systematically evaluate the control performance of each controller, the four evaluation criteria defined. : normalized peak displacement (J_1), normalized peak inter node drift (J_2), normalized peak acceleration (J_3), normalized peak force generated by all control devices (J_4).

The control performance of the LQG control algorithm in reducing the responses of the cantilever beam will be demonstrated through numerical simulation. A 1kg AMD (mass ratio of 5%) will be installed on the top of the structure. A tuned mass damper with no damping ratio and the frequency tuned to the first mode will be used in the simulation. An AMD can be simply modeled by connecting actuator between the tuned mass damper and the top of the structure to provide control force acting on the structure. For the actuators, the maximum force capacity and the maximum stroke are unlimited. The variations of each evaluation criteria for increasing weighting parameters are studied. The response quantities of the structure with the LQG controller are presented in Table 1. As shown Table 1, the AMD system reduces the maximum displacements and internode drifts of the structure by approximately 75-90% of the uncontrolled values. The maximum accelerations is also approximately 65-80% smaller than the uncontrolled values.

The control performance of gyroscope system in reducing the responses of the cantilever beam will be demonstrated through numerical simulation. Two gyroscope systems will be installed on the top of the structure. A pair of gyroscope systems, whose flywheels rotate in the opposite directions, are used to eliminate torsional moment. The gyroscope system has a flywheel rotating speed of 1500rpm and a mass of 0.5kg. The moment of inertia of a flywheel is $0.0025 kg \cdot m^2$.

The response quantities of the structure with LQG controller are presented in Table 2. As shown Table 2, the gyroscope system reduces the maximum displacements and inter-node drifts of the structure by approximately 70-85% of the uncontrolled values. The maximum accelerations is also approximately 65-80% smaller than the uncontrolled values. The overall performance of gyroscope is less than that of the AMD. But this results show that gyroscope system has the possibility to reduce the vibration.

6. Conclusions

Characteristics of a vibration control system utilizing gyroscope system and its effectiveness in the control of earthquake and wind induced vibration were studied. Numerical analysis for a scaled cantilever beam was carried out. The numerical example shows that the gyroscope system has the possibility to reduce the vibration. The performance of the gyroscope system is proportional to rotating speed and moment of inertia of flywheel. The moment of inertia of flywheel is proportional to square of radius of flywheel if flywheel is circular disk. Therefore, mass of control system can be reduced by increasing radius of flywheel.

This system has a potential for application to towers, cranes, high-rise buildings and other structures with prominent bending modes. Furthermore, this system is more compact and has smaller mass than other control devices with the same ability to control

Table 1 Evaluation criteria of AMD

Earthquake	El centro	Hachinohe	Gebze	Mexico
J_1	0.1139	0.1566	0.2128	0.2059
J_2	0.1206	0.1690	0.2415	0.2040
J_3	0.2805	0.1903	0.2913	0.3552
J_4	0.0175	0.0090	0.0179	0.0056

Table 2 Evaluation criteria of gyroscope system

Earthquake	El centro	Hachinohe	Gebze	Mexico
J_1	0.1317	0.1526	0.2837	0.2059
J_2	0.1500	0.1690	0.3250	0.2375
J_3	0.3227	0.1977	0.3489	0.3014
J_4	0.0222	0.0121	0.0122	0.0048

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